Introduction to Krylov subspace methods - 20h Cours-TD

2eme année : Majeure Mathématique : Département Informatique Mathématiques Appliquées

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